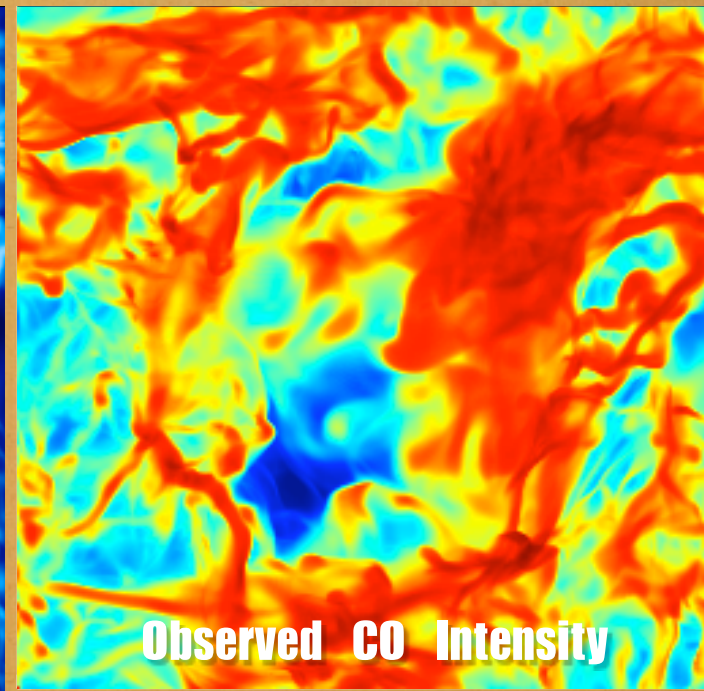
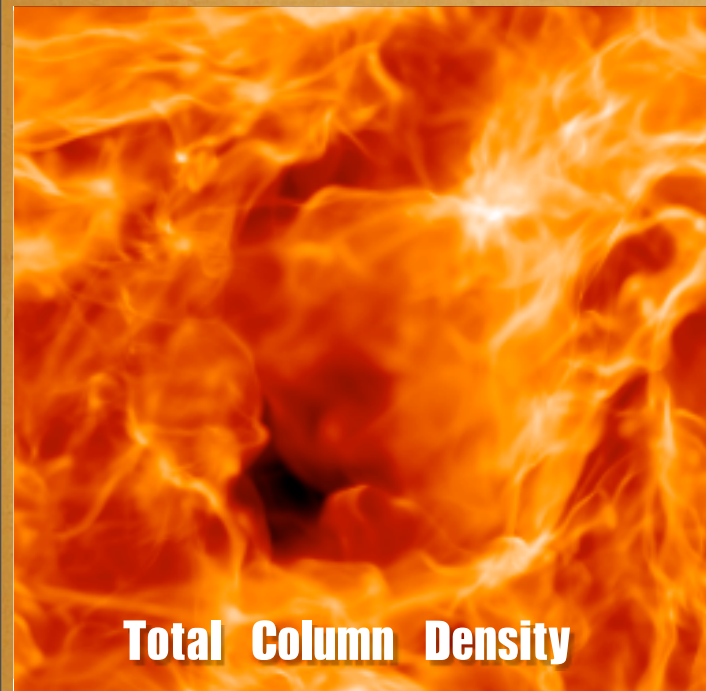


UNDERSTANDING THE X FACTOR IN MOLECULAR CLOUDS

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SIMON GLOVER¹, CORNELIS DULLEMOND¹, RALF
KLESSEN¹, EVE OSTRIKER², ANDREW HARRIS³, BRANDON
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GÖTTINGEN - 9 OCTOBER, 2012

OVERVIEW

- **BACKGROUND: X FACTOR & STAR FORMATION LAW**
- **RADIATIVE TRANSFER IN MHD-CHEMICAL MODELS OF MOLECULAR CLOUDS**
- **RESULTS: THE X FACTOR IN VARIOUS ENVIRONMENTS**
- **RESULTS: THE STAR FORMATION LAW**
- **SUMMARY**

THE X FACTOR

- RATIO OF H₂ COLUMN DENSITY TO ¹²CO INTENSITY FOUND TO BE ~ CONSTANT IN GALACTIC MOLECULAR CLOUDS
 - ⇒ $X = N_{\text{H}_2} / W = 2 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$
(DICKMAN 1978, SOLOMON ET AL. 1987)
- VIRIALIZED MOLECULAR CLOUDS (LARSON 1981, SOLOMON ET AL. 1987)
- Υ -RAY OBSERVATIONS (STRONG & MATTOX 1996)
- DUST BASED OBSERVATIONS (DAME ET AL. 2001, PINEDA ET AL. 2008)
- LOWER METALLICITY (E.G. SMALL MAGELLANIC CLOUD):
- GALACTIC X WHEN CO OBSERVATIONS COMBINED WITH ASSUMPTION OF VIRIALIZED CLOUDS (BOLATTO ET AL. 2008)
- VARYING X DUE TO LARGE QUANTITIES OF H₂ UNTRACED BY CO (RUBIO ET AL. 2004, ISRAEL 1997, LEROY ET AL. 2009, 2010)

OBSERVATIONALLY DERIVED X FACTOR

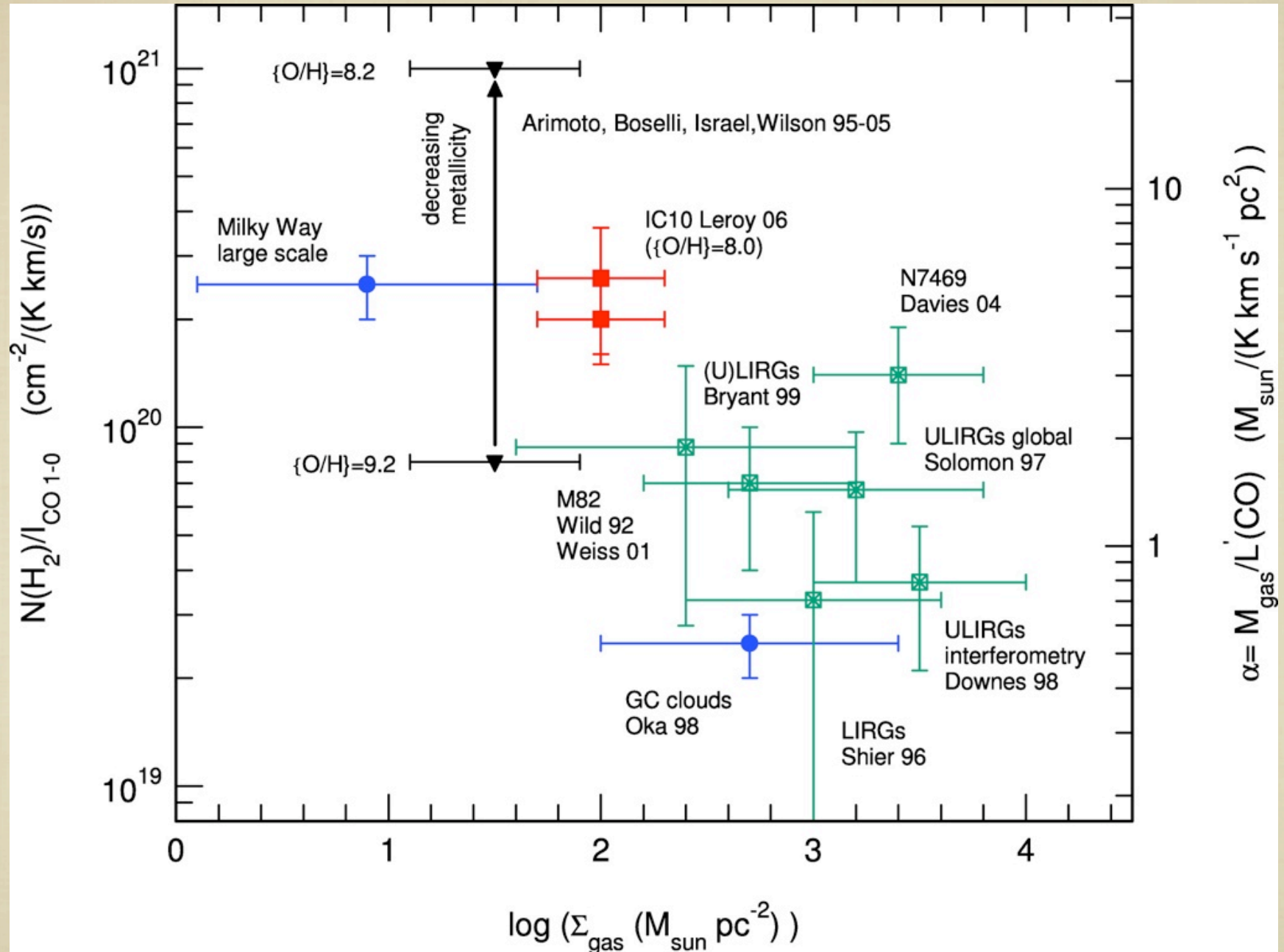
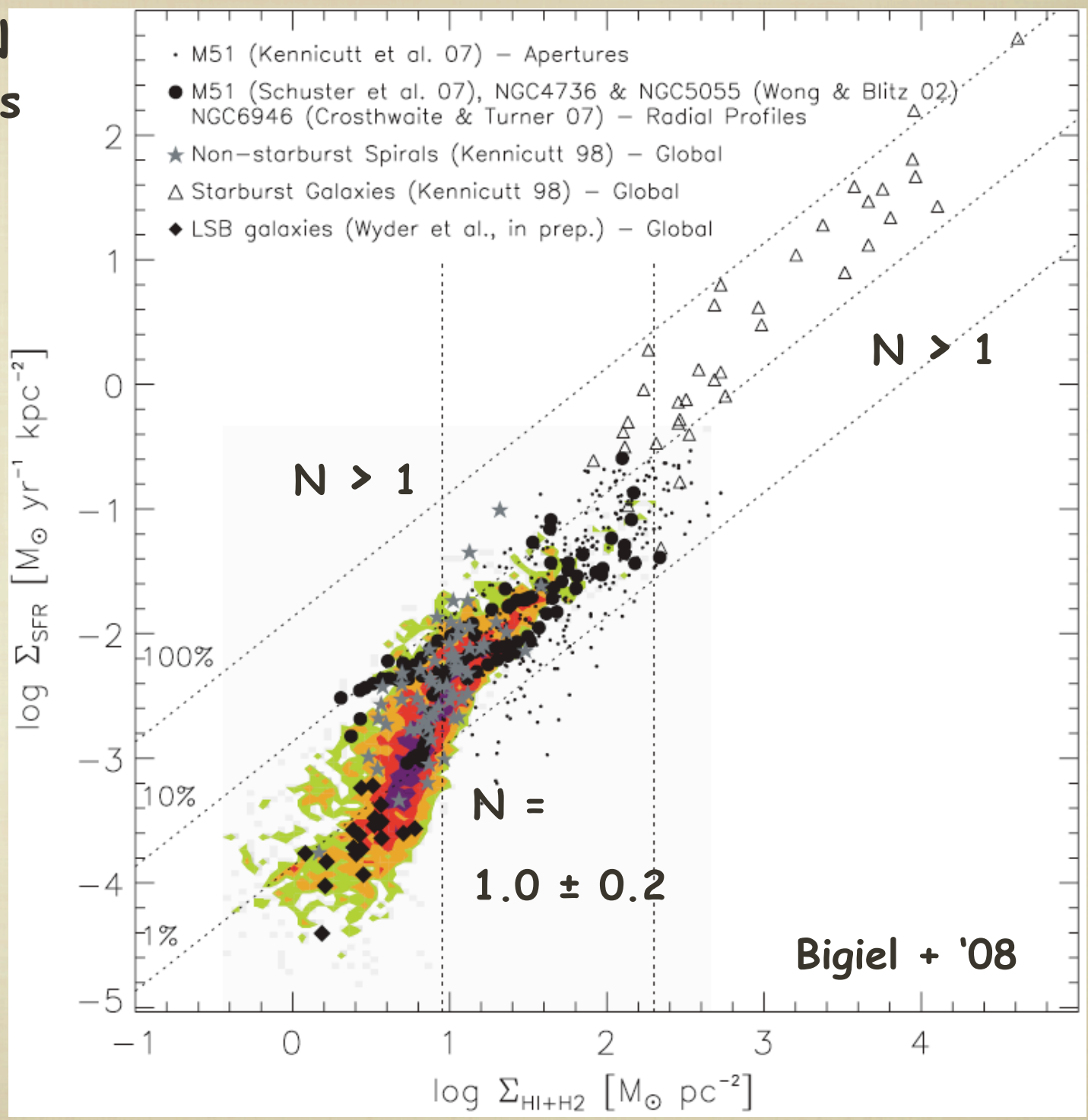


FIGURE FROM TACCONI ET AL. 2008

SF: OBSERVATIONS

$$\square \quad \Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^N$$

- Schmidt '59
- Buat + '89
- Kennicutt '89
- Kennicutt '98
- Hunter + '98
- Boselli + '02
- Wong & Blitz '02
- Boissier + '03
- Heyer + '04
- Leroy + '05
- Kennicutt + '07
- Leroy + '08
- Bigiel + '08
- Blanc + '09
- Verley + '10
- Daddi + '10
- Genzel + '10
- ...

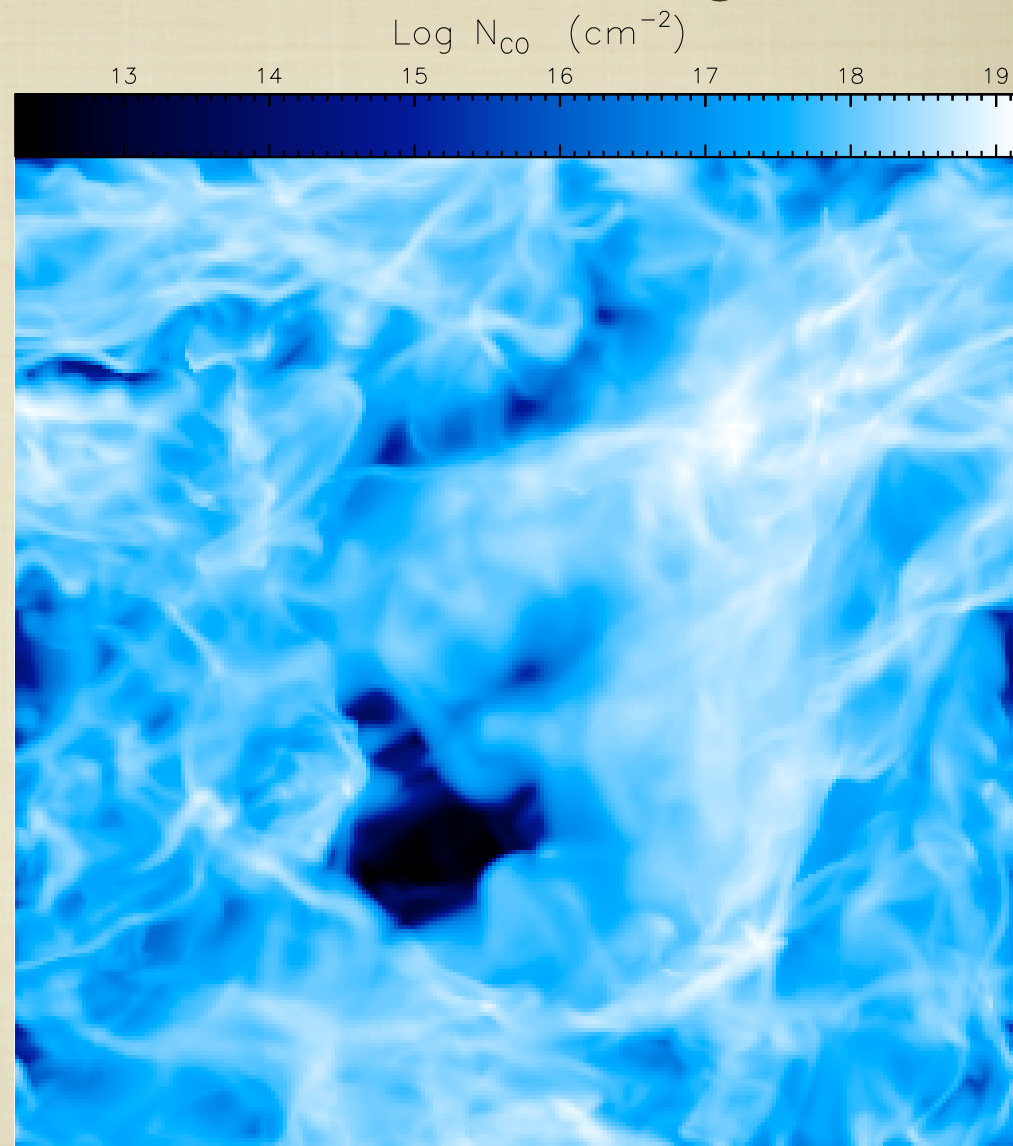
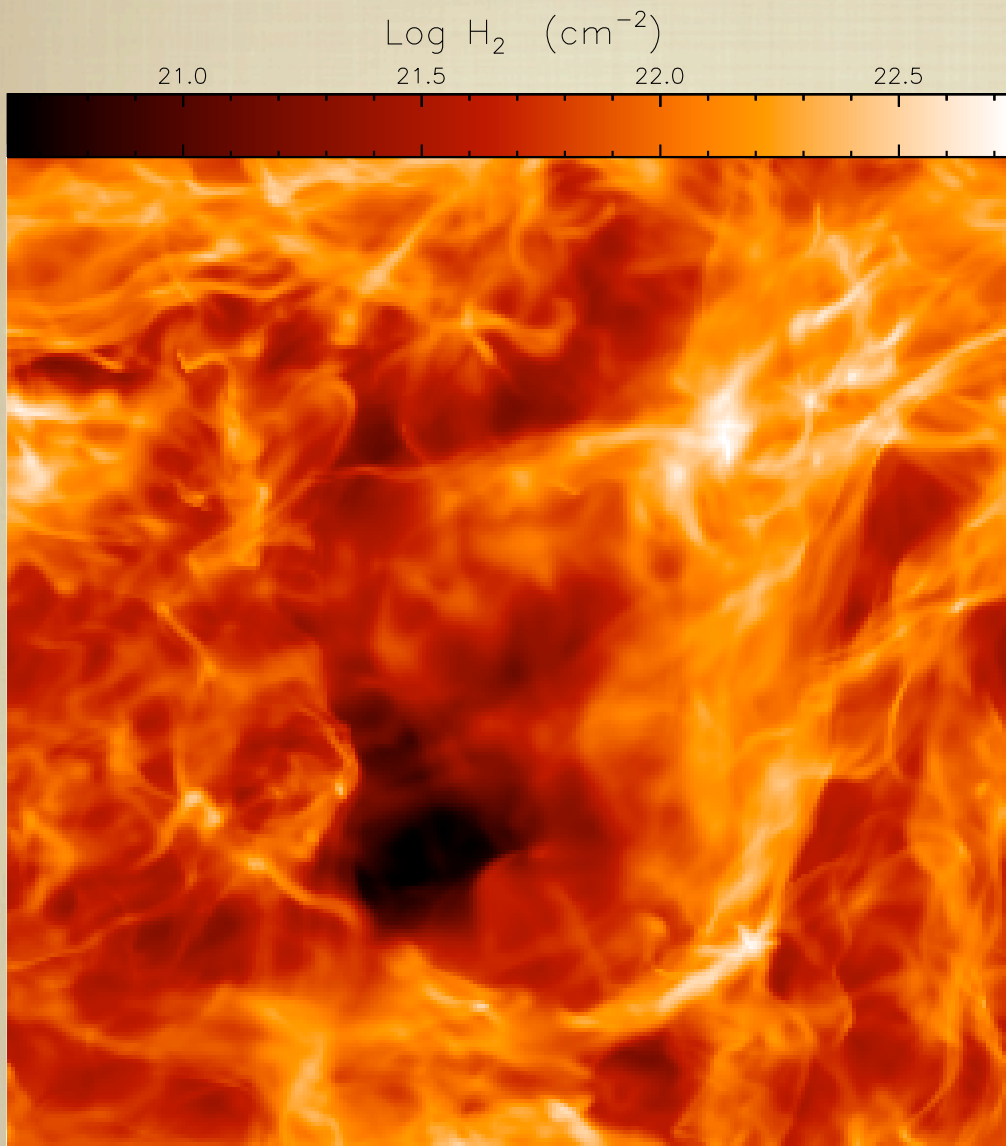


MODELING CO FORMATION

- GLOVER ET AL. 2010: SELF-CONSISTENT TREATMENT OF CHEMISTRY IN MHD MOLECULAR CLOUD SIMULATIONS
 - MHD ($B_0 = 1.95 \mu\text{G}$); DRIVEN TURBULENCE
 - TRACK 218 REACTIONS OF 32 SPECIES
 - CO FORMATION VERY SENSITIVE TO MC PROPERTIES: BACKGROUND RADIATION FIELD, DENSITY AND METALLICITY (VAN DISHOECK & BLACK 1988, MALONEY & BLACK 1988)
 - H_2 FORMATION MAINLY DEPENDENT ON CLOUD AGE (GLOVER & MAC LOW 2011)
- LVG RADIATIVE CALCULATIONS TO MODEL CO INTENSITY, AND THE X FACTOR (SHETTY ET AL. 2011A,B)

CO IN MCS

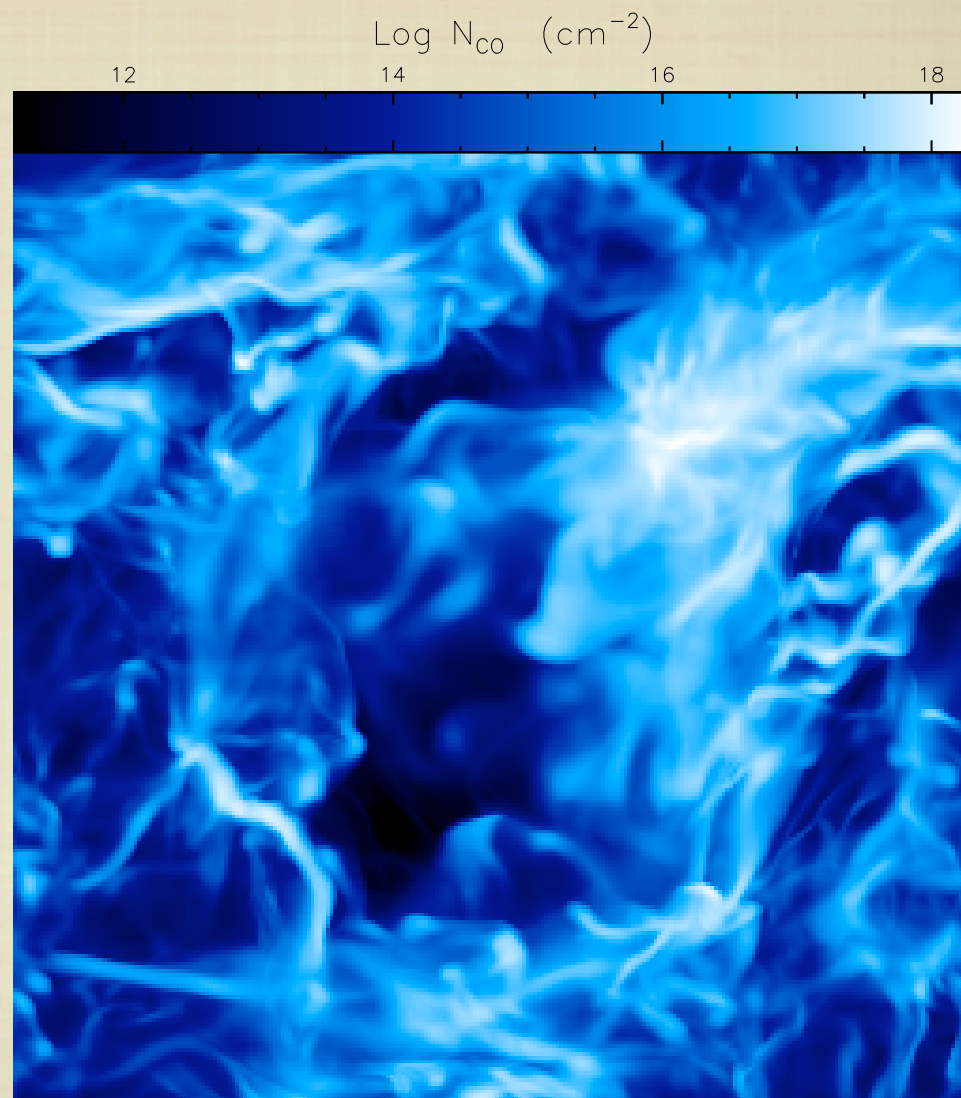
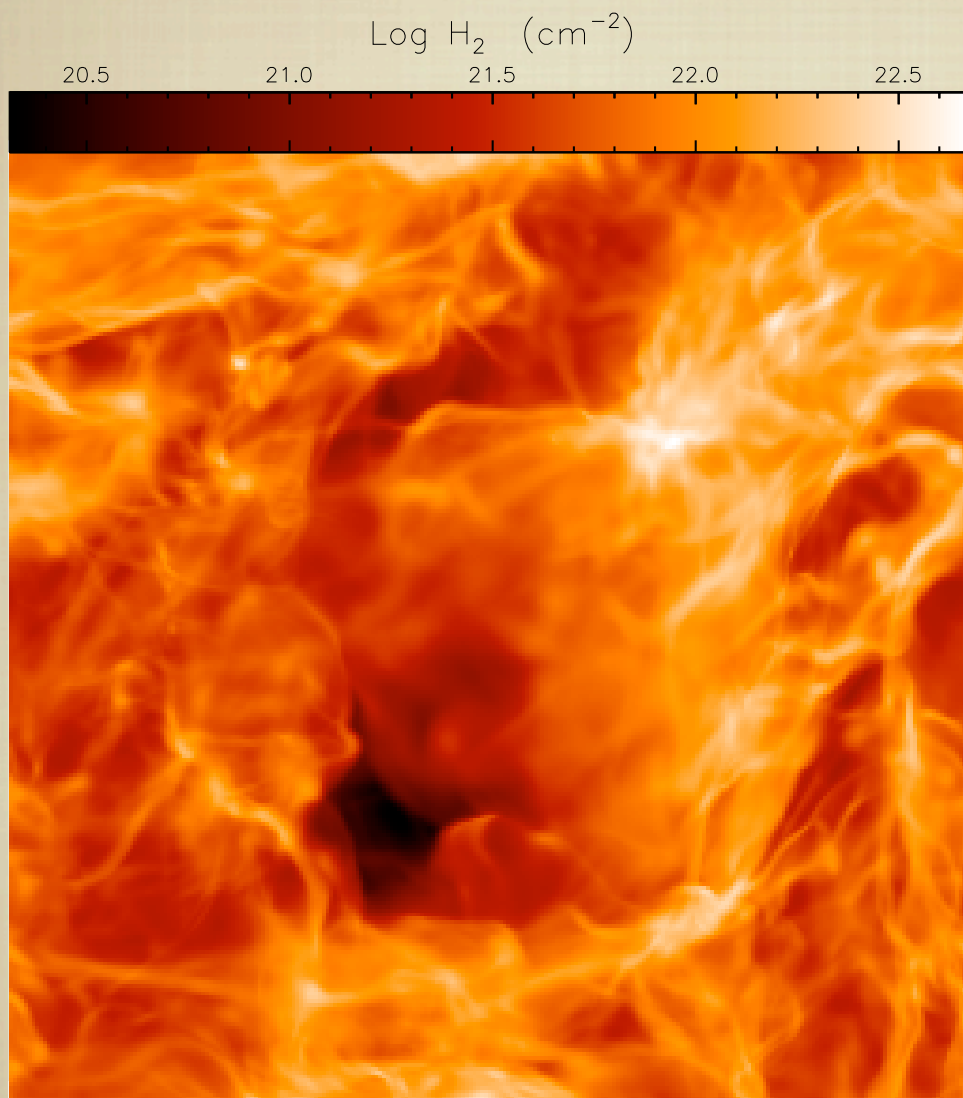
MODEL MILKY WAY CLOUD: $n_0=300 \text{ cm}^{-3}$, $Z=Z_{\odot}$



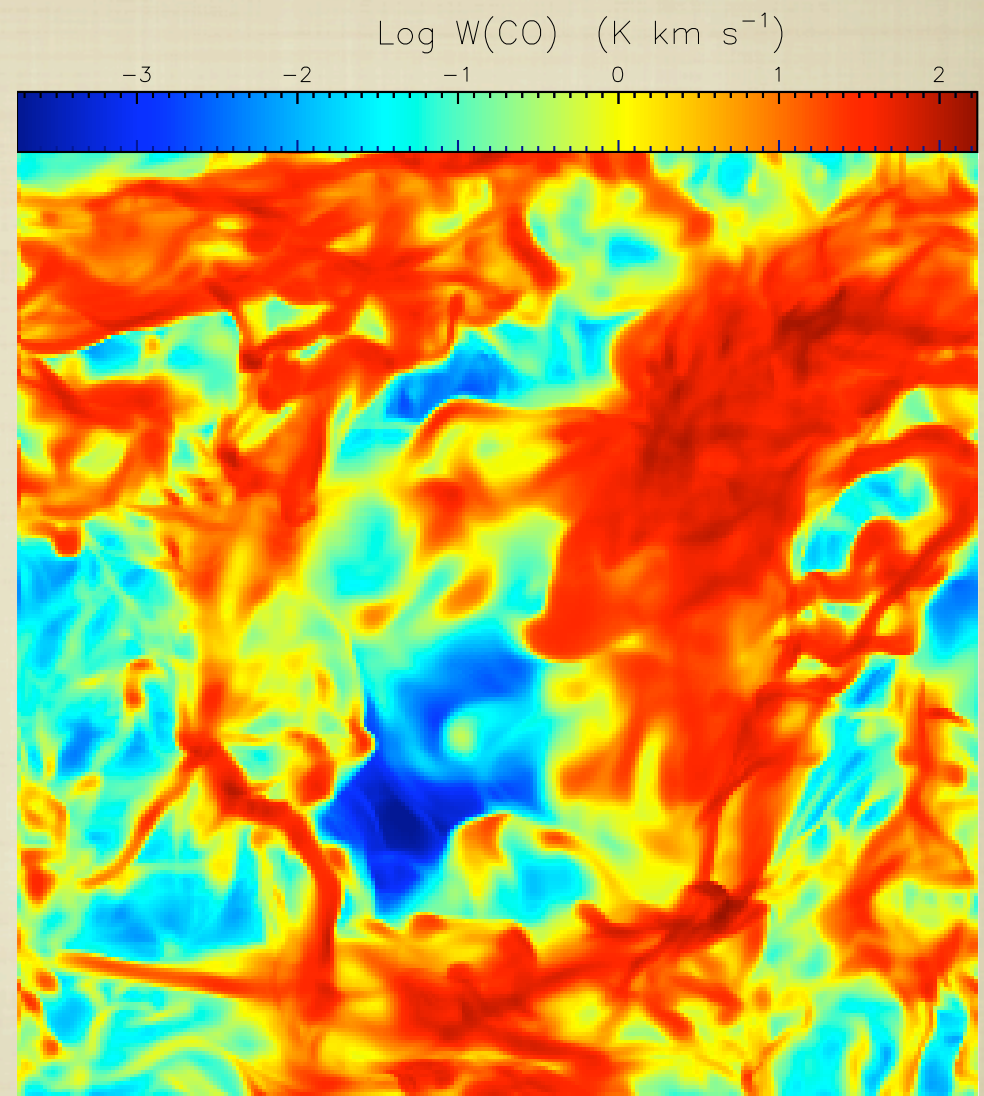
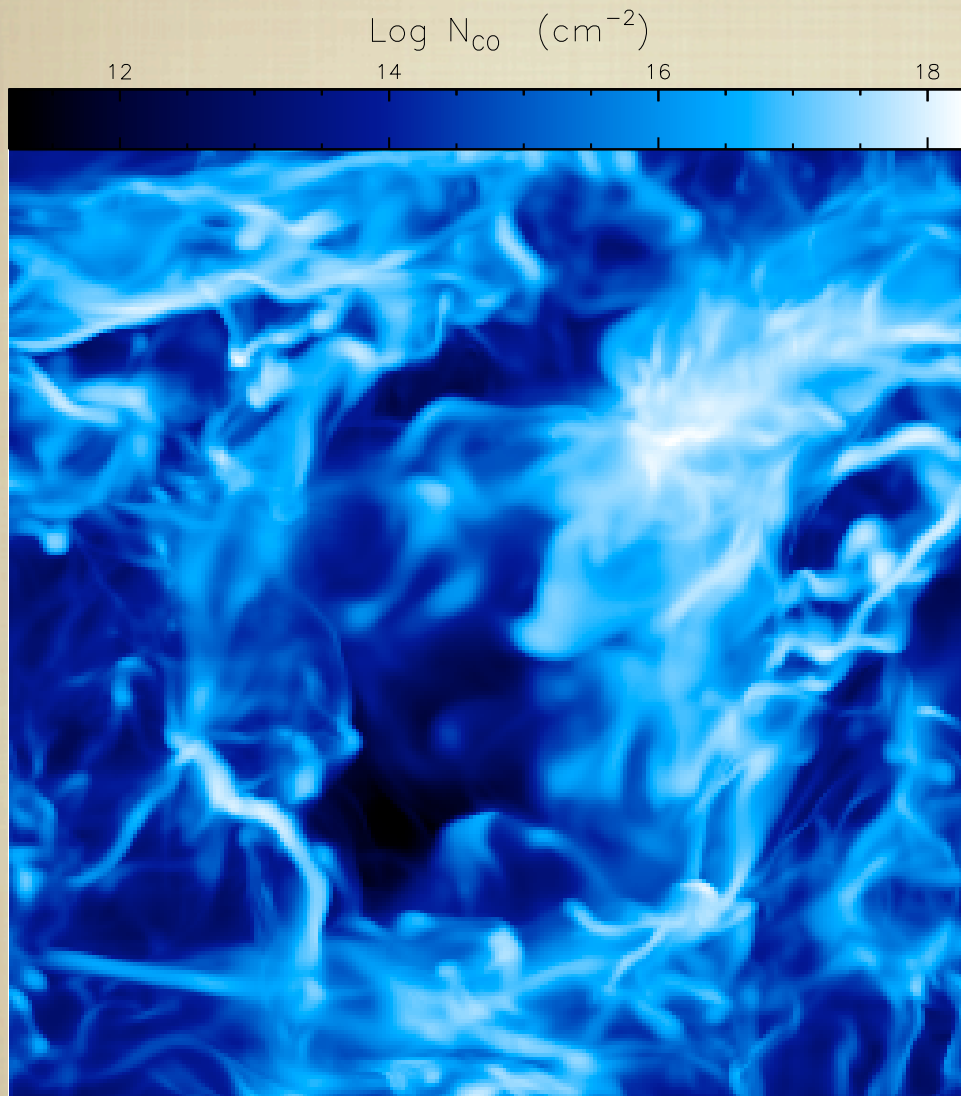
20 PC

GLOVER ET AL. (2010)

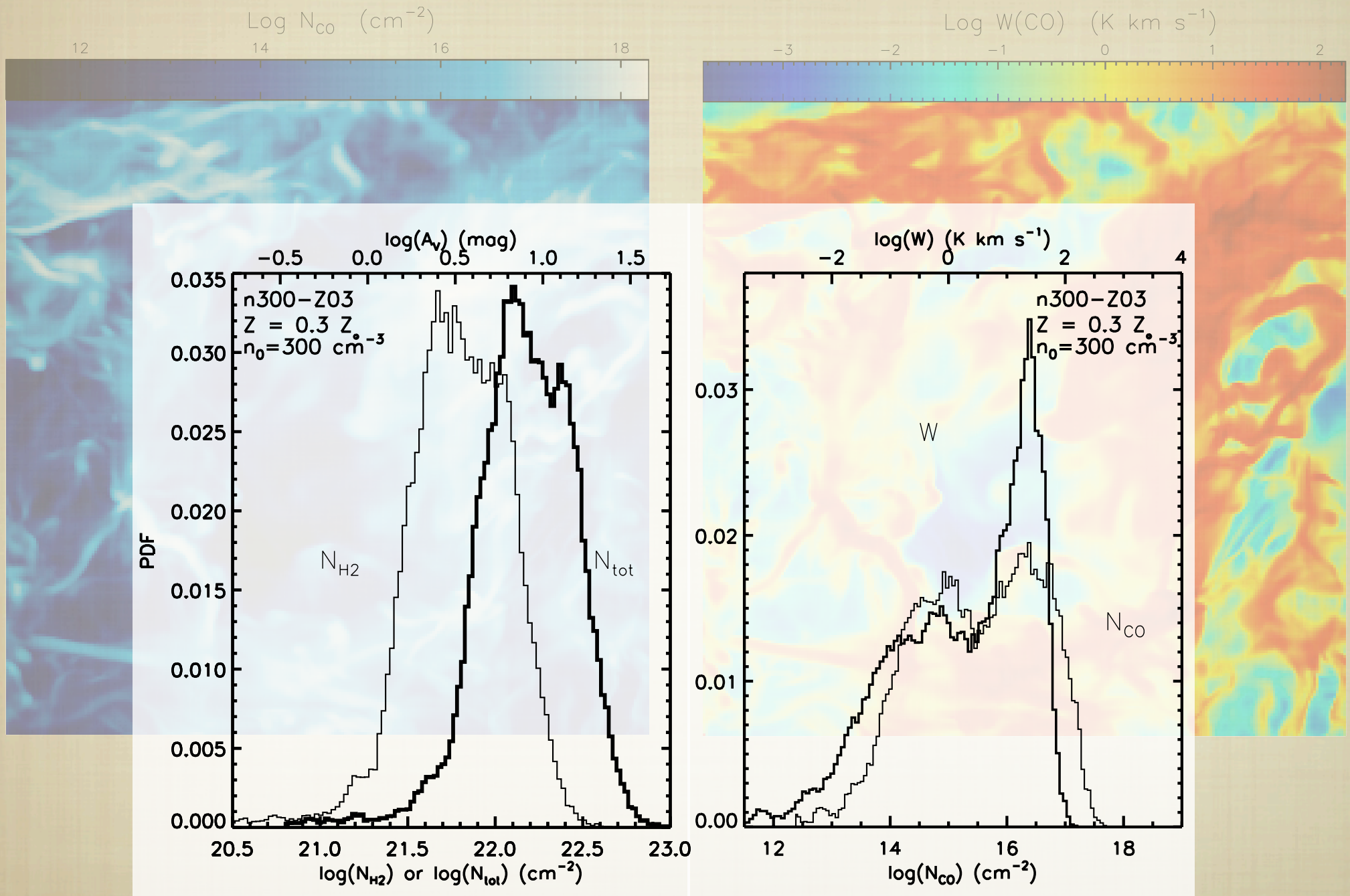
CO IN LOW METALLICITY MCS $Z=0.3$ Z_{\odot}



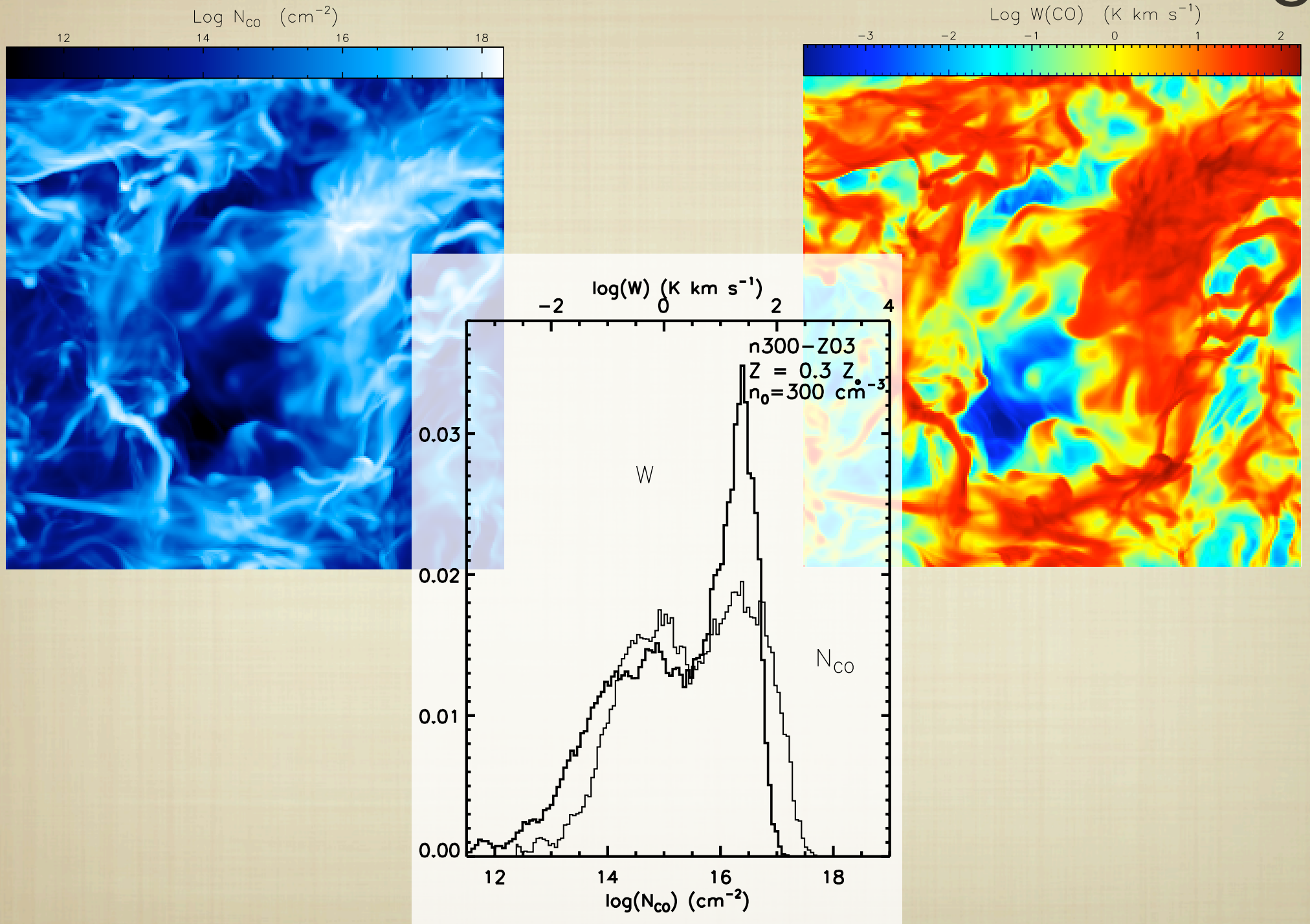
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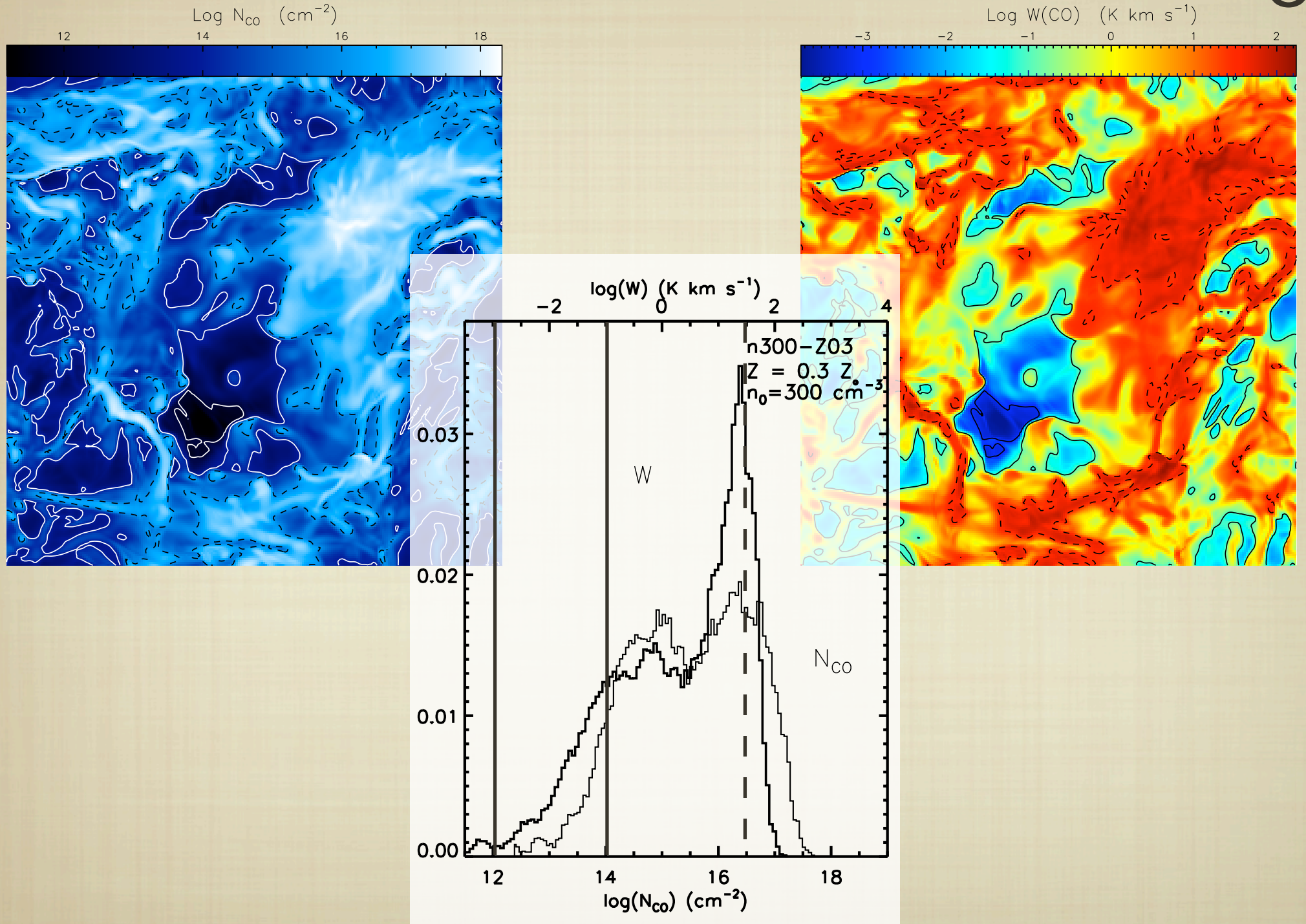
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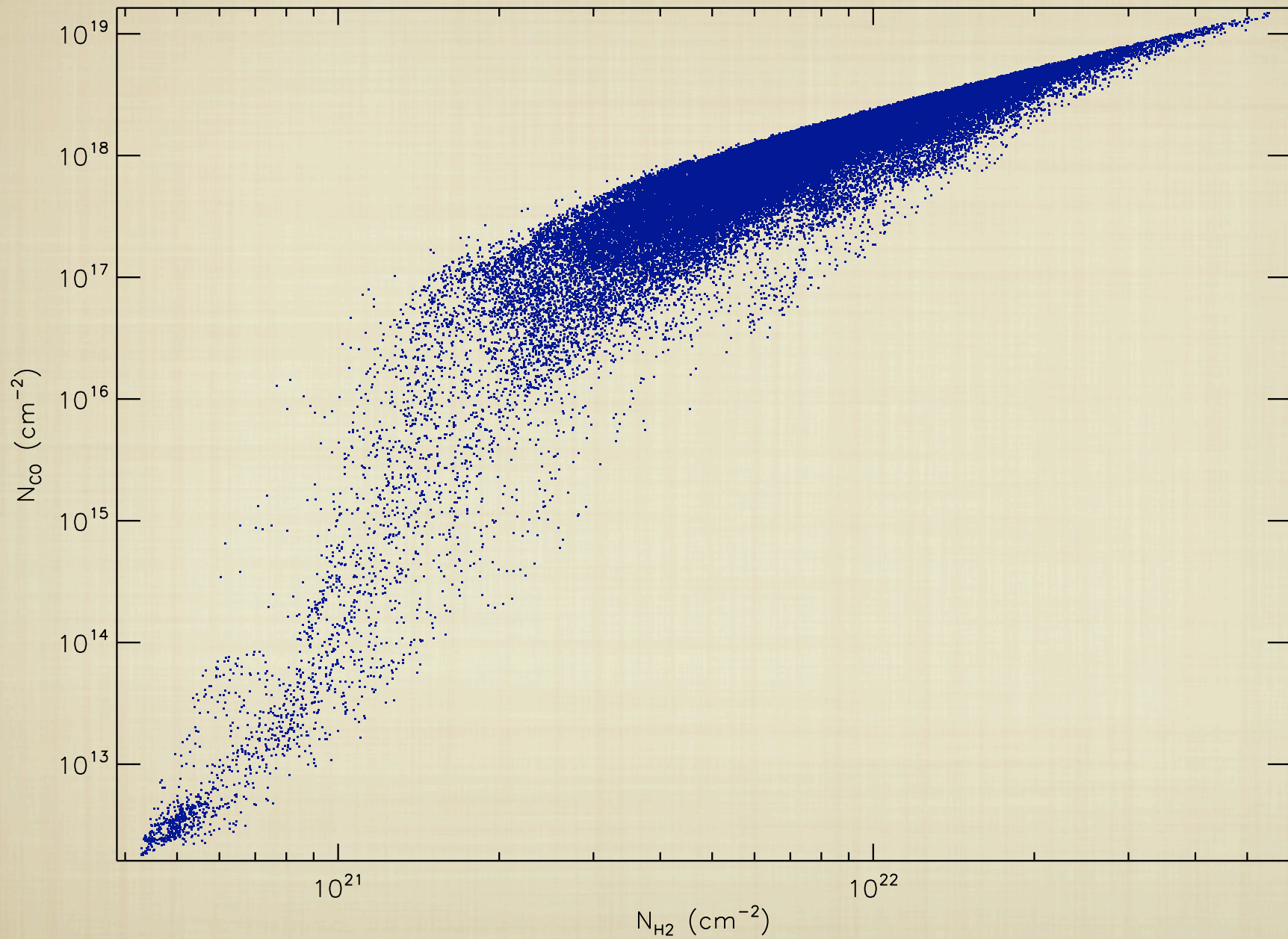
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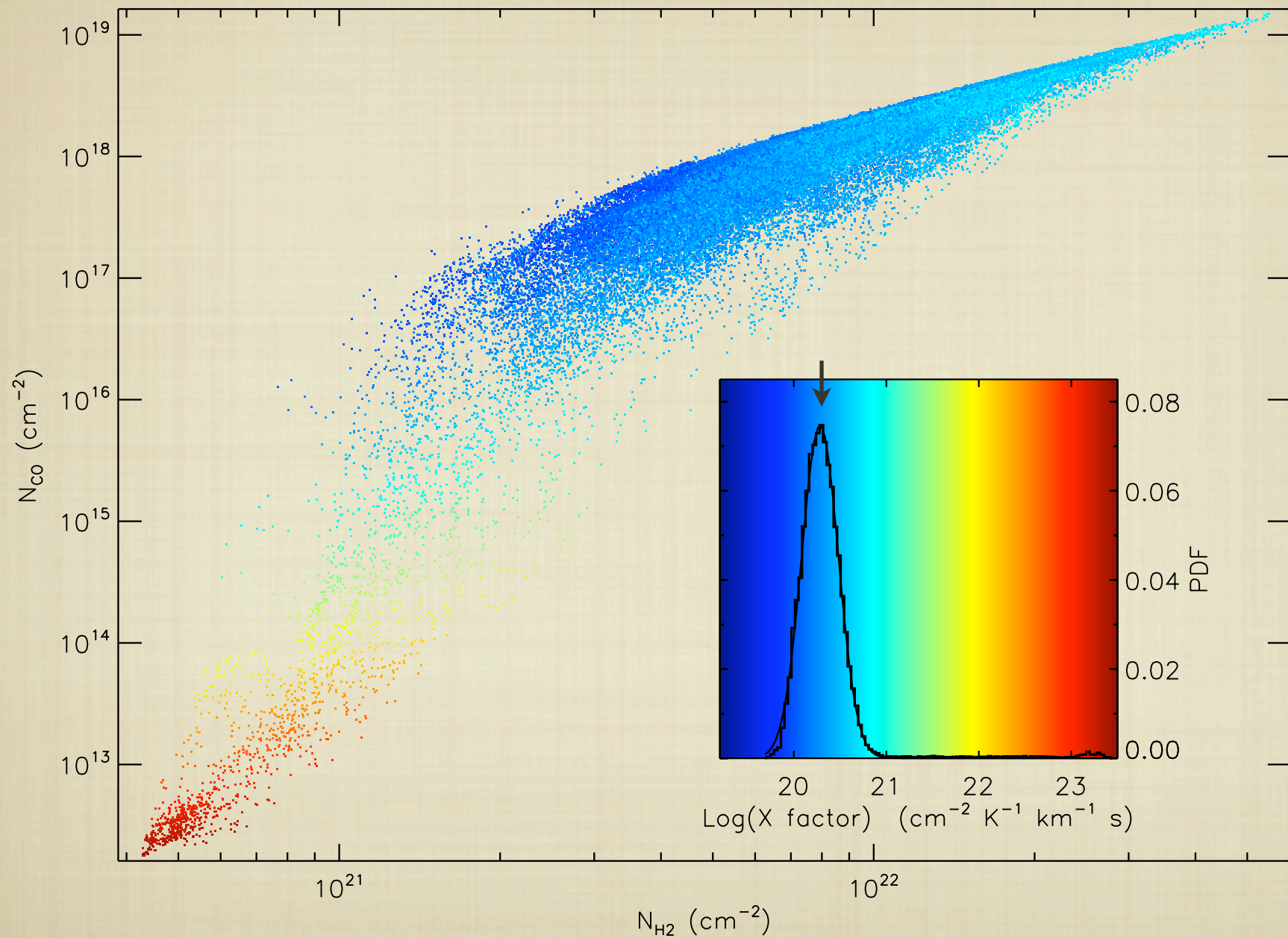


THE X FACTOR = N_{H_2}/W



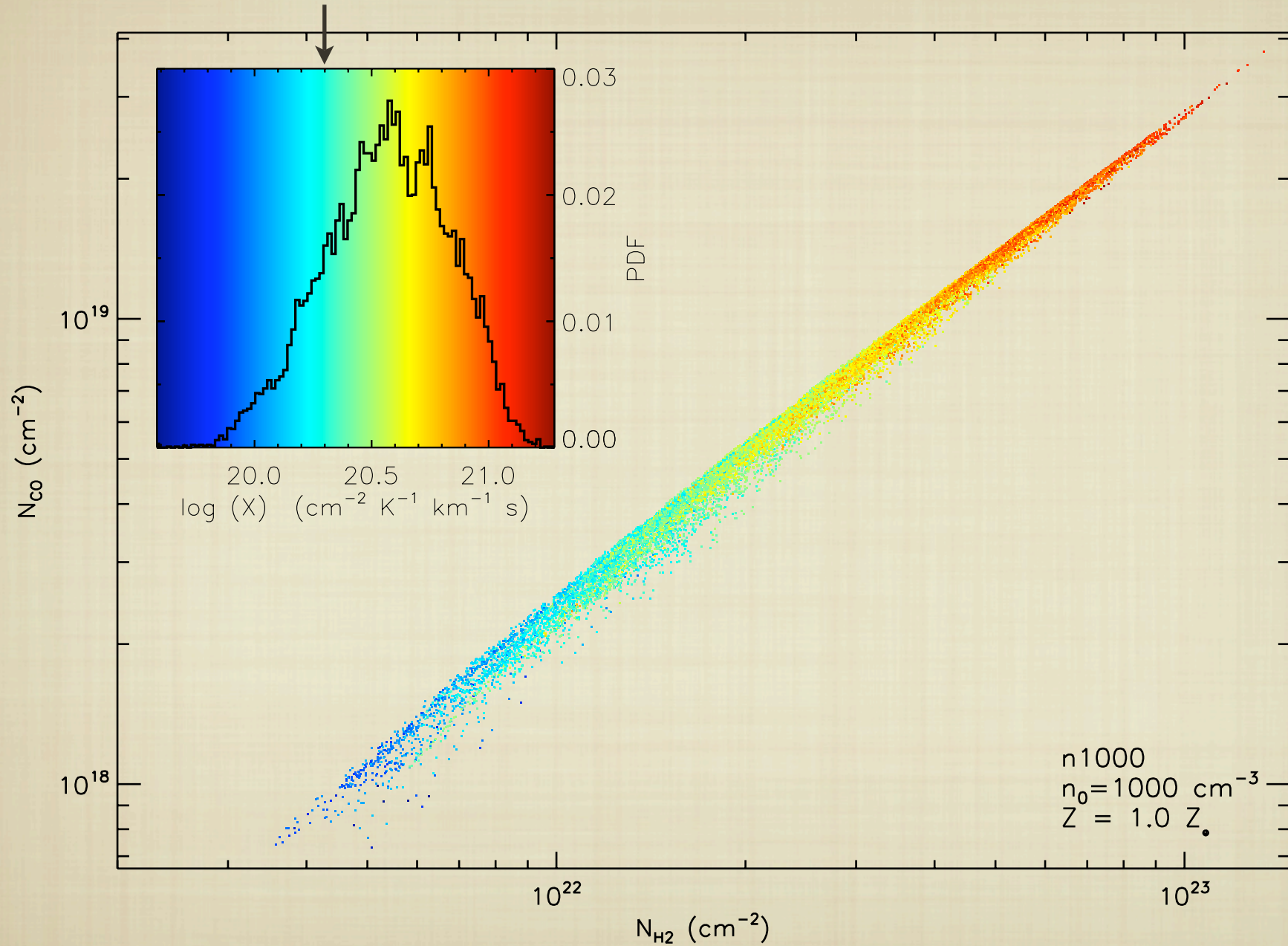
SHETTY ET AL. (2011A)

THE X FACTOR = N_{H_2}/W



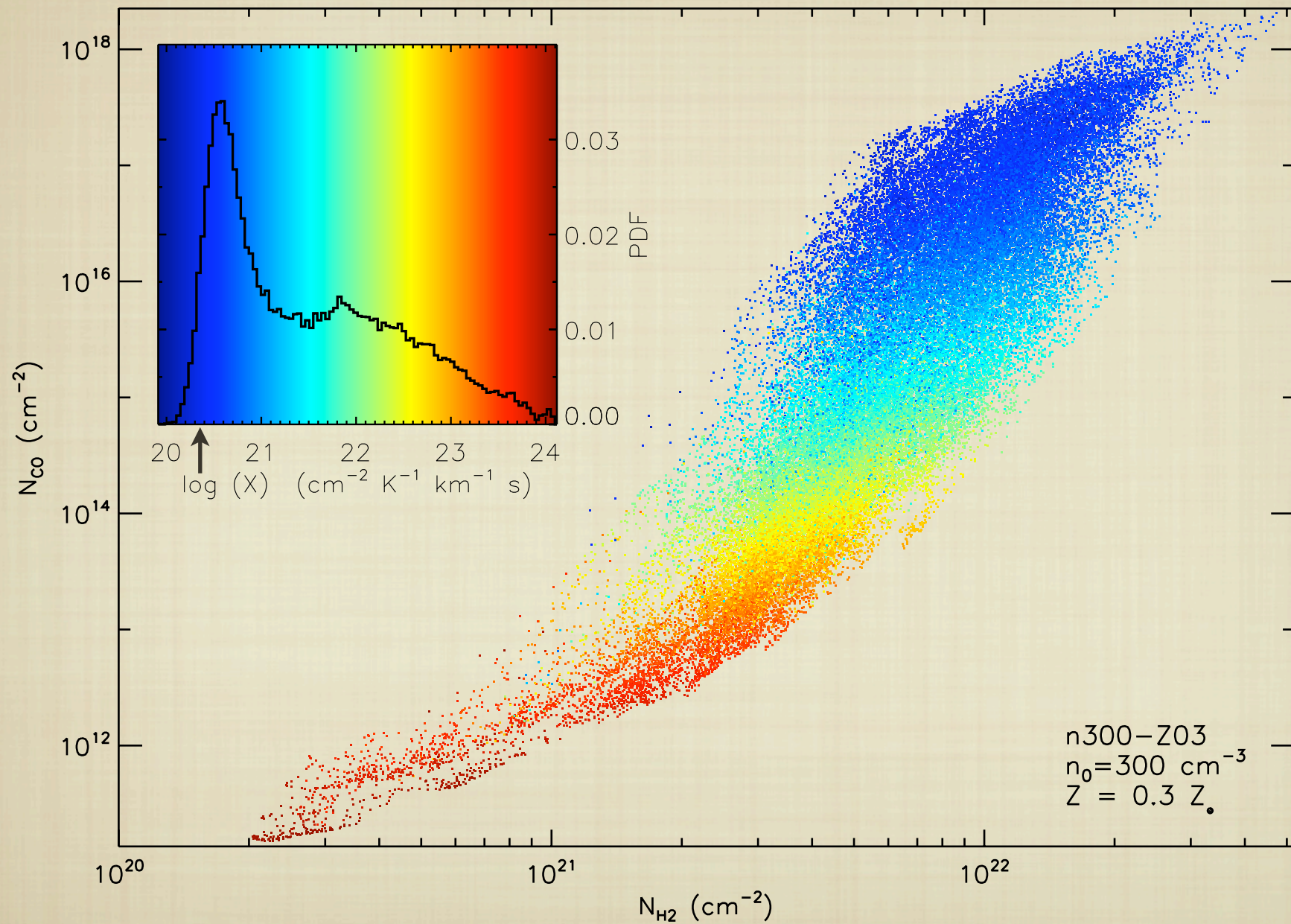
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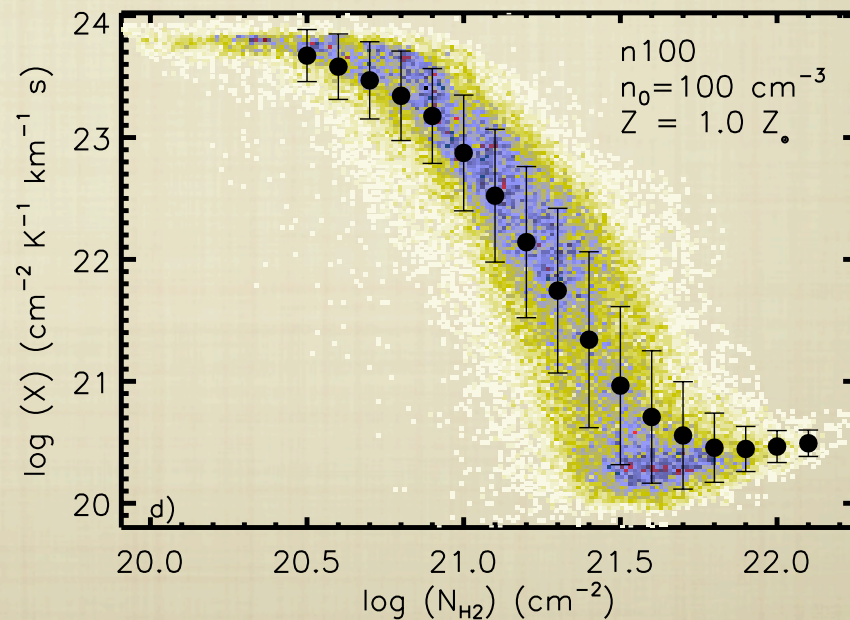
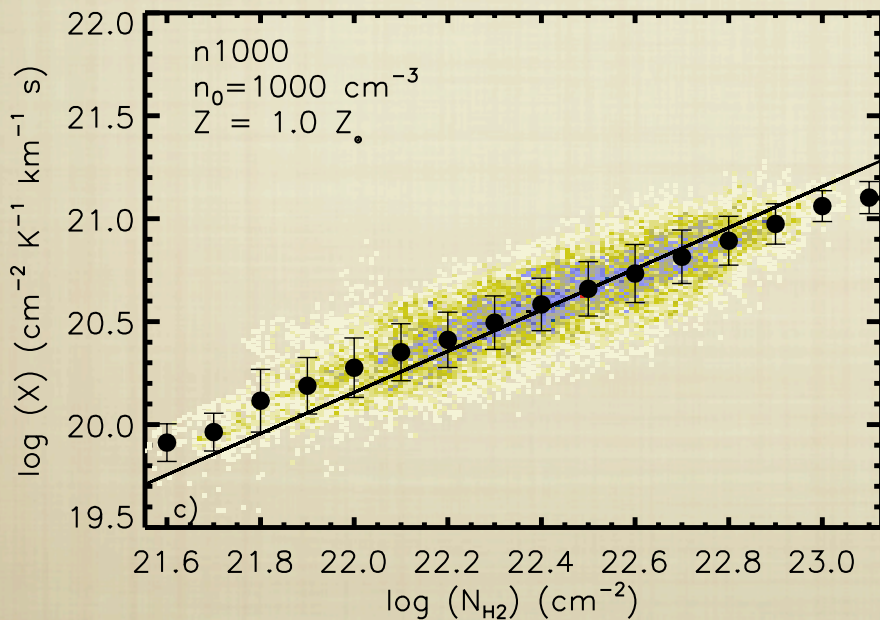
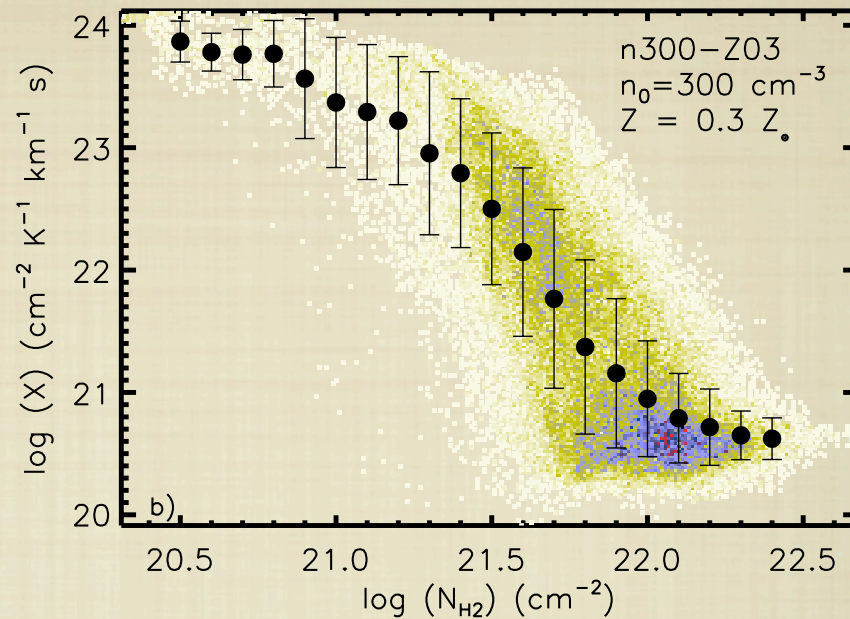
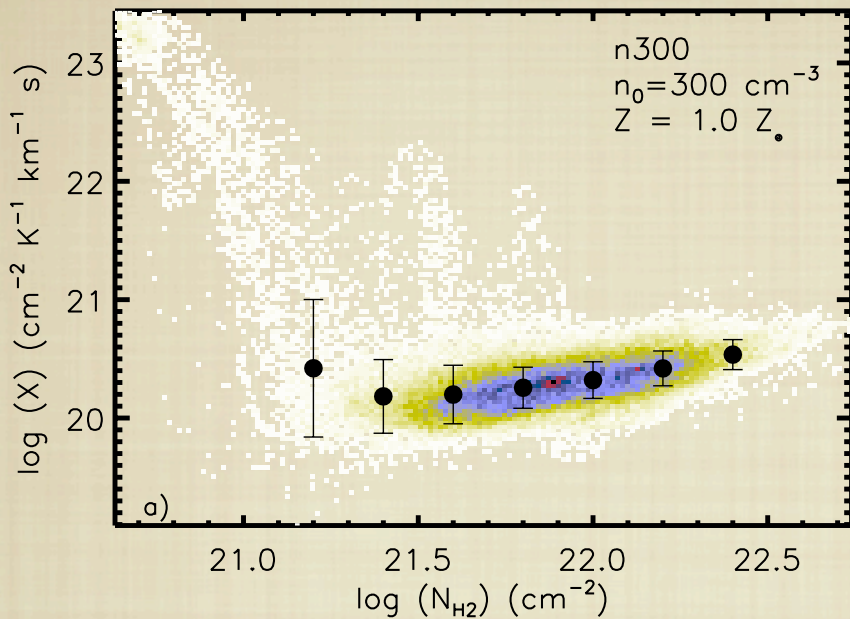
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OBSERVATIONALLY DERIVED X FACTOR

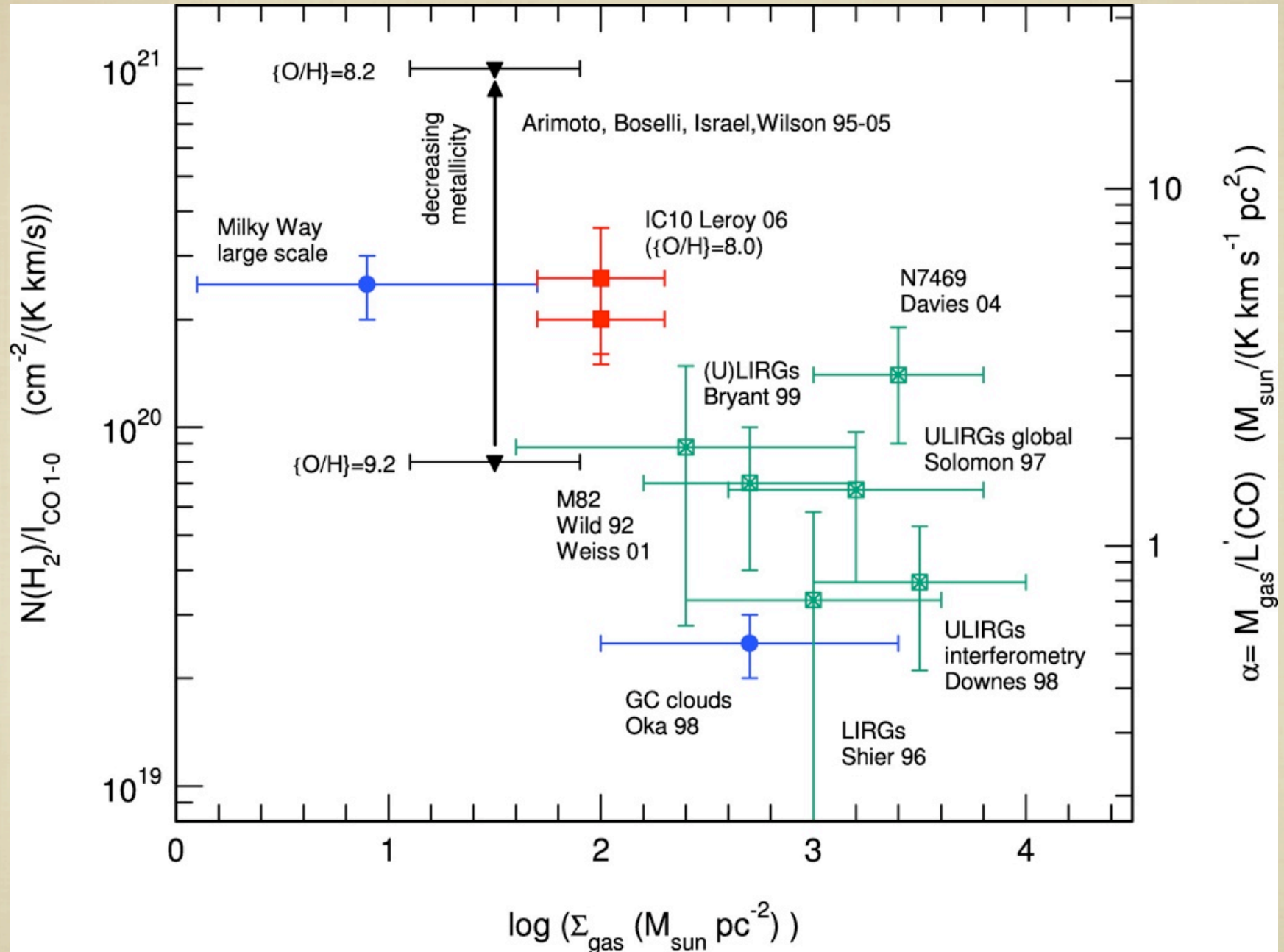


FIGURE FROM TACCONI ET AL. 2008

OBSERVATIONALLY DERIVED X FACTOR

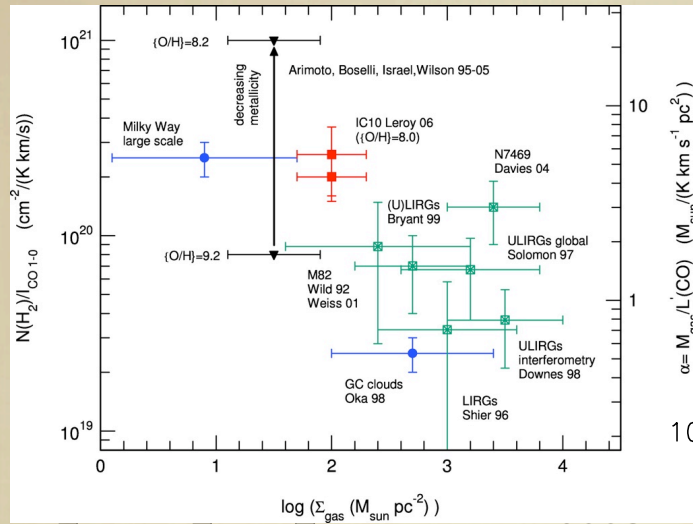
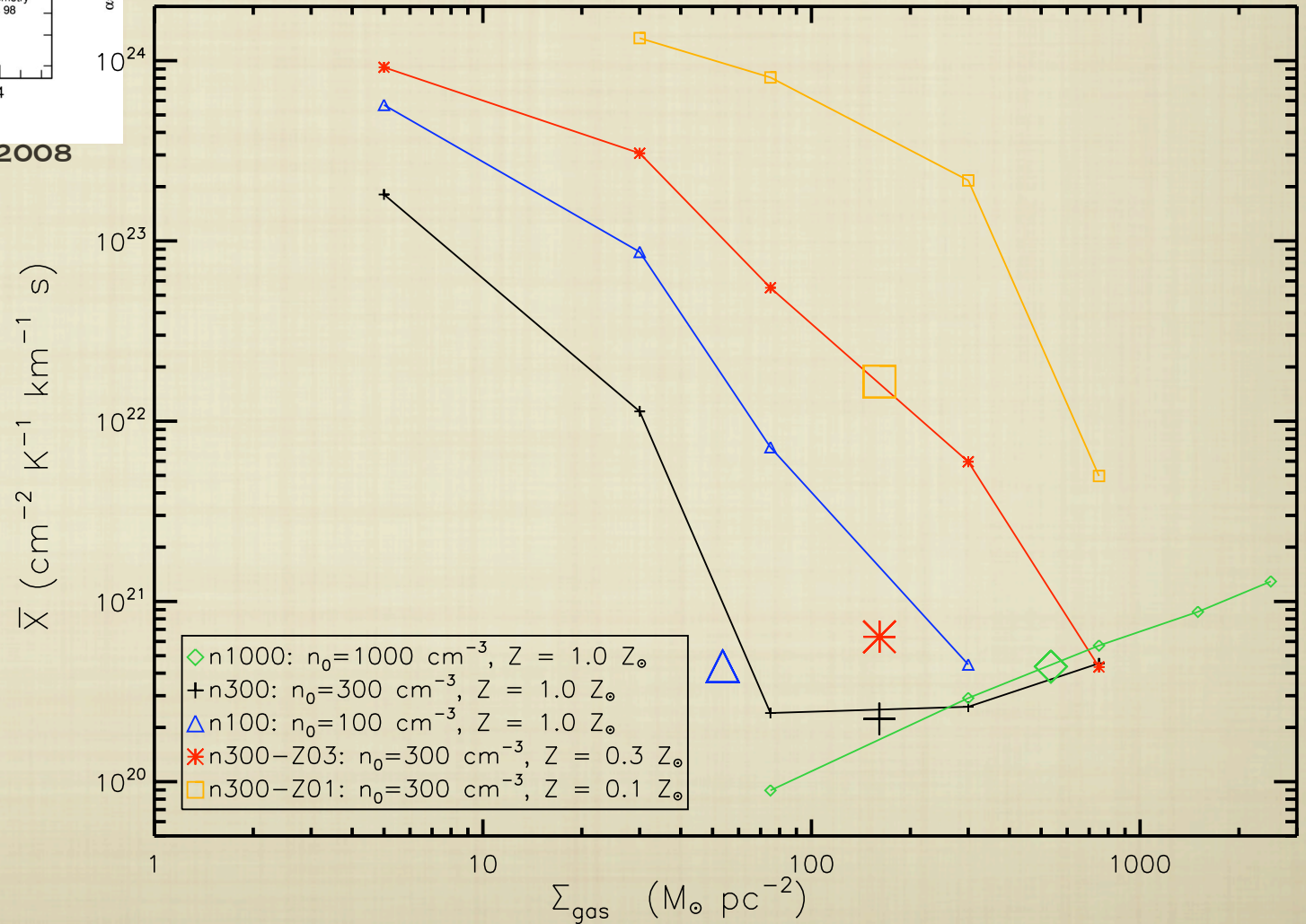


FIGURE FROM TACCONI ET AL. 2008



OBSERVATIONALLY DERIVED X FACTOR

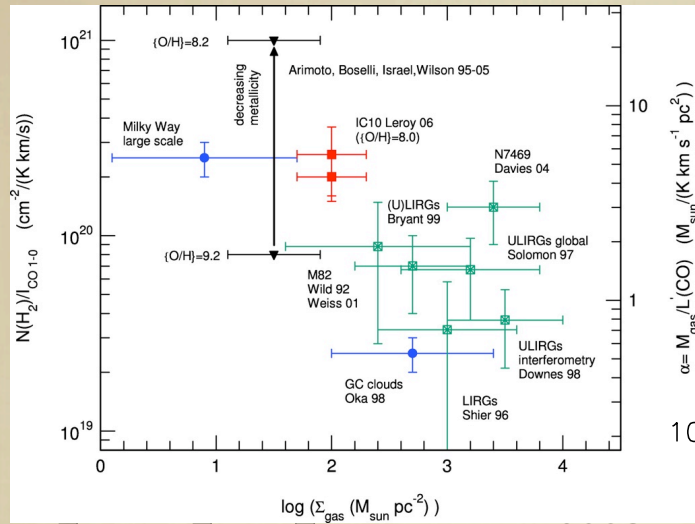
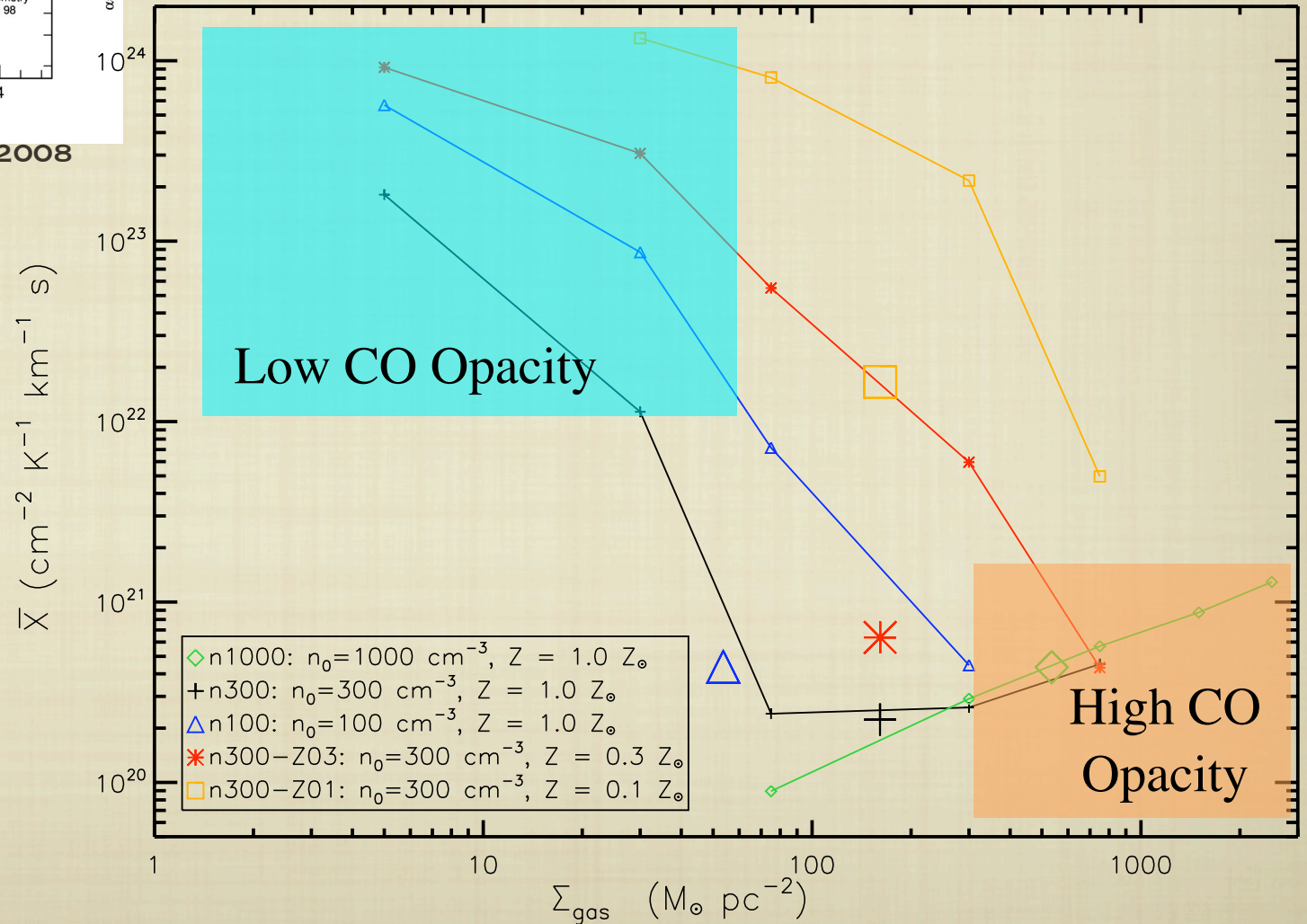


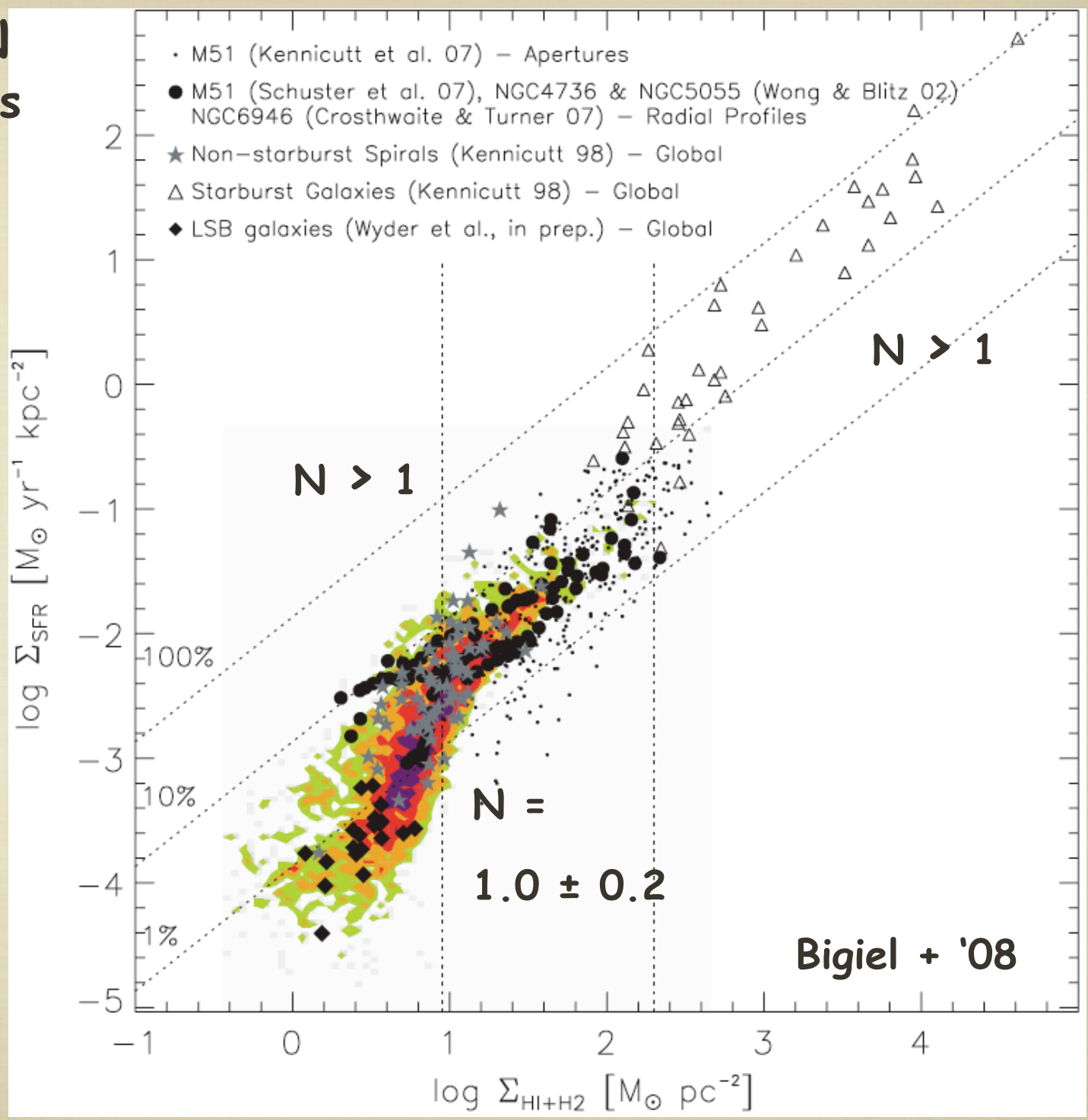
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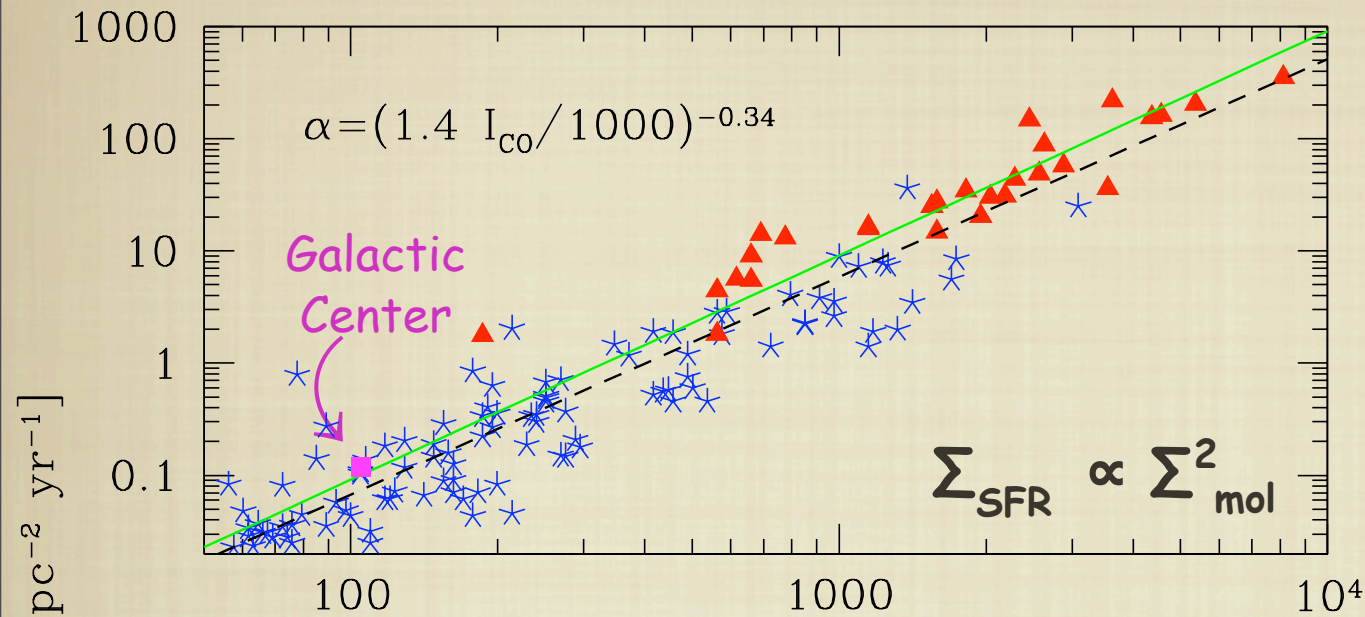
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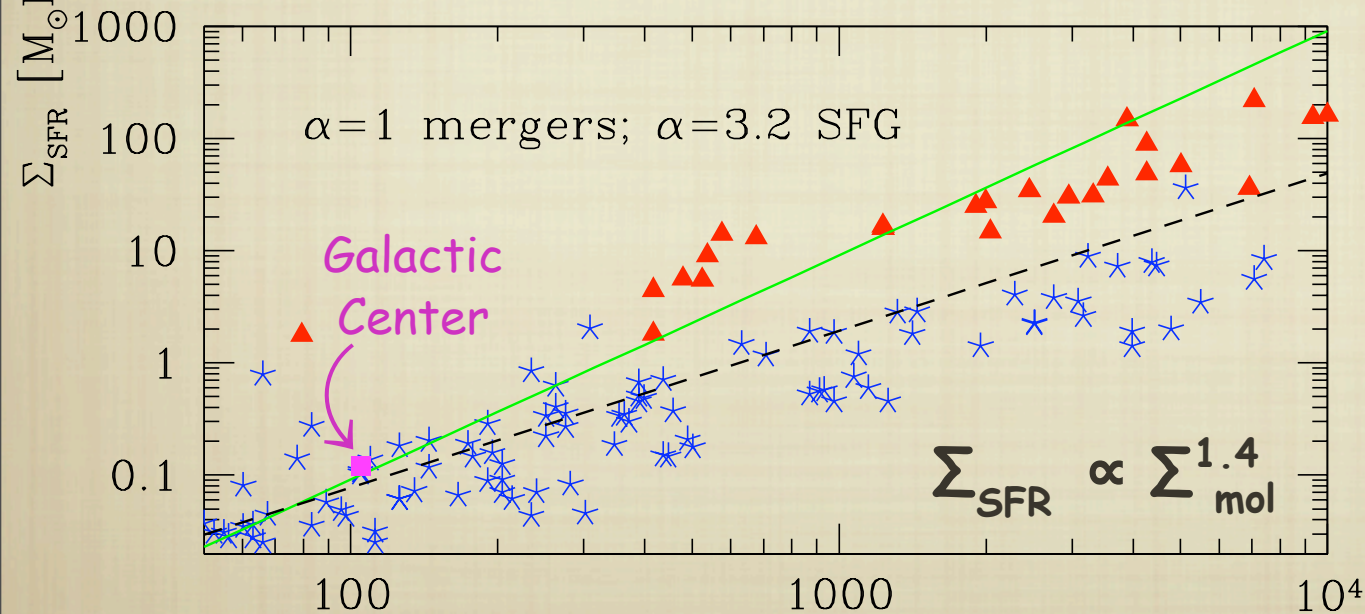


SELF-REGULATION IN OBSERVED SYSTEMS?



Star forming galaxies and merger systems from Genzel + '10

Galactic Center from Yusef-Zadeh + '09



Continuous X factor? (Shetty + 11a,b, Narayanan + 11, 12, Feldmann + '12)

Ostriker & Shetty '11 $\Sigma_{mol} [M_{\odot} pc^{-2}]$

Shetty & Ostriker '12

Inferring the Kennicutt-Schmidt Law

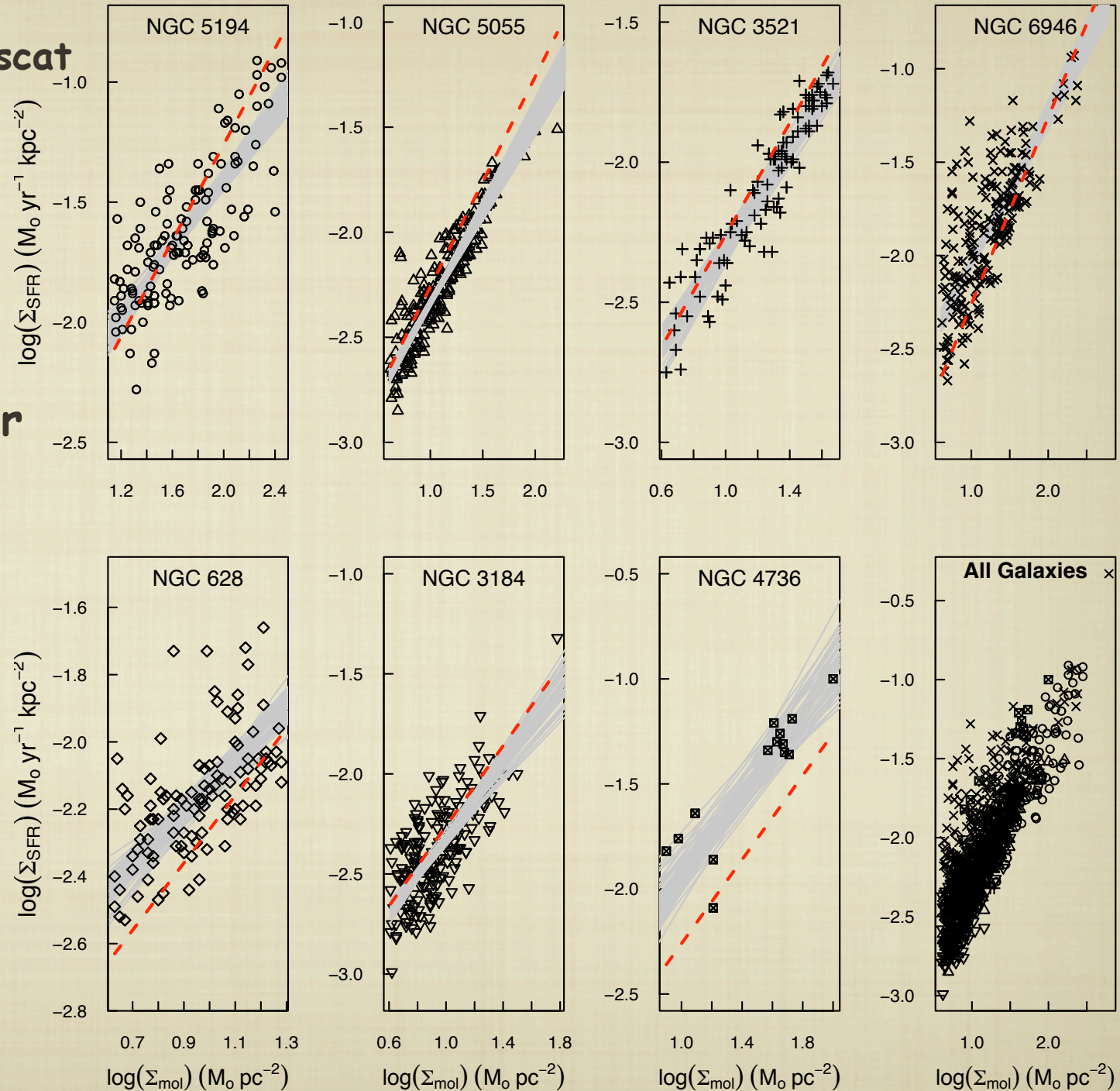
- Measurement uncertainties and intrinsic scatter may lead to biases in fitting a model to data (e.g. Weiner+2006, Kelly 2007).
- Hierarchical models allow for estimating the model parameters of individuals and for the group
- Bayesian inference is ideally suited for fitting hierarchical models, and accounting for uncertainties, through MCMC methods
- Employ a hierarchical Bayesian method, with a full treatment of uncertainties to estimate Kennicutt-Schmidt law parameters from the Bigiel + 2008 sample

Hierarchical Bayesian Fitting of the KS Law

$$\Sigma_{\text{SFR}} = A \Sigma_{\text{mol}}^N + \epsilon_{\text{scat}}$$

fit individual and
"group" parameters,
with uncertainties

Posterior is a PDF
of each fit parameter

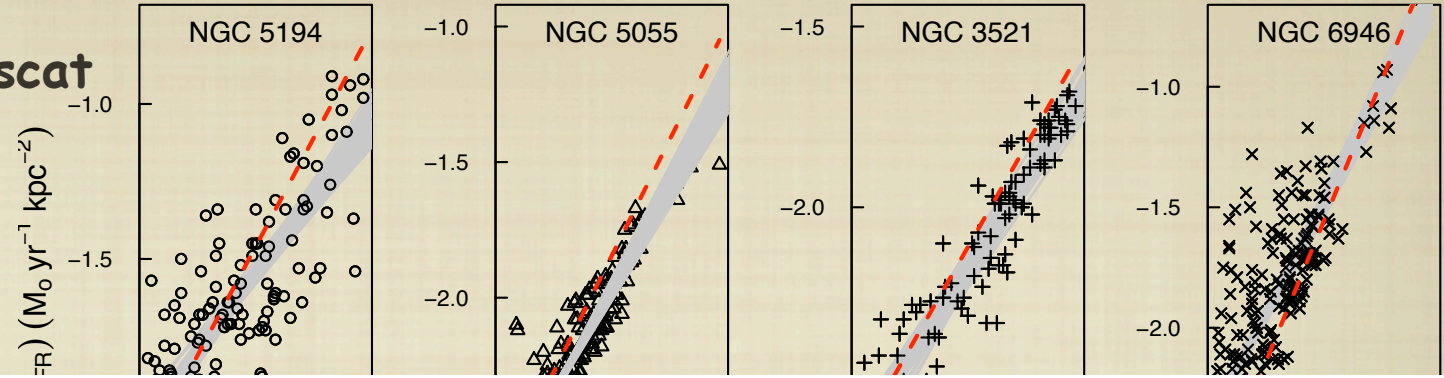


Bigiel+'08, '10
Shetty, Kelly, Bigiel
MNRAS submitted,
arXiv1210:1218

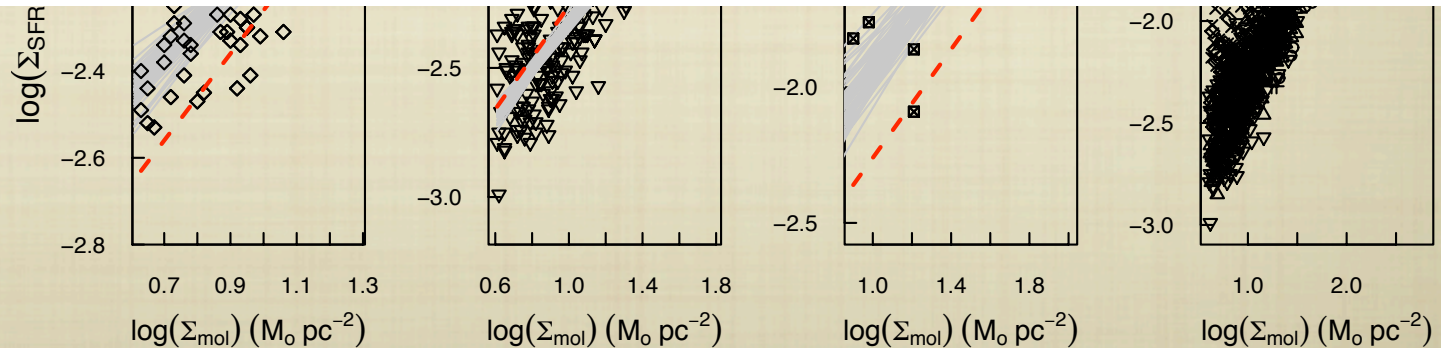
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Subject	Bayes A	Bayes $2\sigma_A$	Bayes N	Bayes $2\sigma_N$	Bayes σ_{scat}
NGC 5194 (M51)	-2.84	[-3.0, -2.7]	0.72	[0.62, 0.83]	0.06
NGC 5055	-3.20	[-3.3, -3.1]	0.87	[0.79, 0.95]	0.04
NGC 3521	-3.20	[-3.4, -3.0]	0.90	[0.76, 1.03]	0.05
NGC 6946	-2.81	[-2.9, -2.7]	0.78	[0.70, 0.86]	0.11
NGC 628	-2.89	[-3.1, -2.6]	0.76	[0.51, 0.95]	0.05
NGC 3184	-3.24	[-3.4, -3.1]	0.92	[0.79, 1.10]	0.05
NGC 4736	-2.83	[-3.2, -2.4]	0.92	[0.67, 1.20]	0.08
Group Parameters	-3.00	[-3.3, -2.7]	0.84	[0.63, 1.0]	0.14



Bigiel+'08, '10
Shetty, Kelly, Bigiel
MNRAS submitted,
arXiv1210:1218

SUMMARY

- X FACTOR VARIES WITH ENVIRONMENT, DEPENDING ON METALLICITY, MEAN DENSITY, AMBIENT UV FIELD, ETC...
- AT LOW METALLICITY, NEED A HIGHER X FACTOR
→ MORE “DARK GAS”
- KENNICUTT-SCHMIDT RELATIONSHIP STRONGLY DEPENDENT ON X FACTOR
- SUPER-LINEAR KS INDEX AT HIGH SURFACE DENSITIES (E.G. STARBURSTS) DUE TO SELF-REGULATION
- IN NORMAL GALAXIES, NO UNIVERSAL KS LAW
- SUB-LINEAR KS RELATIONSHIP FROM HIERARCHICAL BAYESIAN FIT, SUGGESTIVE OF CO EMISSION FROM GAS UNASSOCIATED WITH STAR FORMATION

INTERPRETATION OF THE X FACTOR

■ CONSTANT X DUE TO “VIRIALIZED” CLOUDS? (SOLOMON ET AL. 1987)

$$X \propto \alpha_{VT} \equiv \frac{M_{VT}}{L_{CO}}$$

■ VELOCITY - MASS RELATIONSHIP FOR CLOUDS IN VIRIAL EQUILIBRIUM (BERTOLDI & MCKEE 1992):

$$\sigma_{VT}^2 \equiv \frac{GM_{VT}}{5R}$$

■ CLOUD AVERAGED SPECTRA ARE GAUSSIAN:

$$L_{CO} = \sqrt{2\pi} T_{B,0} \sigma_v \pi R^2$$

■ TAKEN TOGETHER (& ASSUMING $\sigma_v = \sigma_{VT}$):

$$\alpha_{VT} \equiv \frac{M_{VT}}{L_{CO}} \propto \frac{\sigma_v / R}{T_{B,0}}$$

■ EQUIVALENTLY:

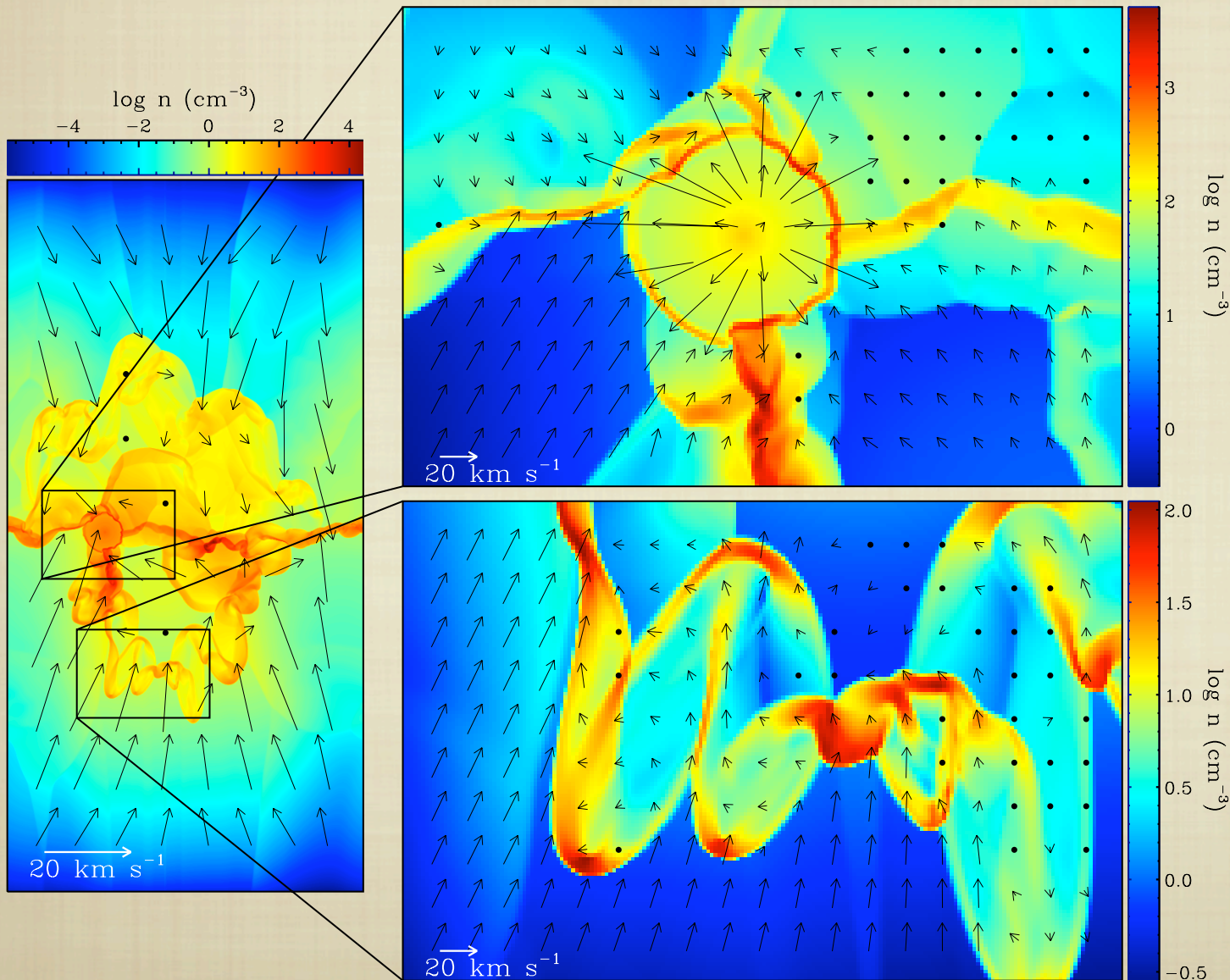
$$\alpha_{VT} \equiv \frac{M_{VT}}{L_{CO}} \propto \frac{\rho^{1/2}}{T_{B,0}}$$

■ VIRIALIZED CLOUDS ALSO INVOKED TO EXPLAIN “LARSON’S (1981) LAWS”: $M \propto R^2$ AND $\sigma_v \propto R^{1/2}$

In Starbursts:

Dynamic Equilibrium: $W_{\text{tot}} \approx P_{\text{drive}} \approx P_{\text{turb}}$

$$\pi G \Sigma^2 / 2 \approx f_p (p^* / 4m^*) \Sigma_{\text{SFR}} \approx \rho \sigma_z^2$$



Ostriker & Shetty '11
Shetty & Ostriker '12